

EXPONENTS AND

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POWERS.

Class: VIII, Mathematics

(F)

SOLUTIONS

TEACHING TASK

$$\begin{aligned} 01. \quad \frac{a^{15} \cdot b^4}{a^6 \cdot b^2} &= a^{15-6} \cdot b^{4-2} \\ &= a^9 \cdot b^2 \end{aligned}$$

Ans: B

$$\begin{aligned} 02. \quad x + y &= 5 \\ \Rightarrow x^2 + y^2 + 2xy &= 25 \\ \Rightarrow 10 + 2xy &= 25 \\ \Rightarrow xy &= \frac{15}{2} = 7\frac{1}{2} \end{aligned}$$

Ans: A

$$\begin{aligned} 03. \quad (a^{4n} \cdot b^{3n} \cdot a^{2n})^2 \\ &= (a^{4n+3n+2n})^2 \\ &= (a^{9n})^2 = a^{18n} \end{aligned}$$

Ans: C

$$\begin{aligned} 04. \quad \left[5 \left(8^{\frac{1}{3}} + 27^{\frac{1}{3}} \right)^3 \right]^{\frac{1}{4}} \\ &= \left[5 (2 + 3)^3 \right]^{\frac{1}{4}} \\ &= \left[5 \times 125 \right]^{\frac{1}{4}} = \left[625 \right]^{\frac{1}{4}} = 5 \end{aligned}$$

Ans: B

$$\left\{ \left(\frac{1}{3} \right)^{-3} - \left(\frac{1}{2} \right)^{-3} \right\} \div \left(\frac{1}{4} \right)^{-3}$$

$$= (27-8) \div 64$$

$$= \frac{19}{64}$$

Ans: A

2

$$(\sqrt[3]{4})^{2x+1} = \frac{1}{32} \quad \Rightarrow \quad \frac{4x+1}{3} = -5$$

$$= 4 \quad \Rightarrow \quad \frac{4x+1}{6} = \frac{-5}{2}$$

$$\Rightarrow 4x+1 = -15$$

$$\Rightarrow x = -4$$

Ans: A

$$08. \quad 3 \cdot a^8 \cdot b^2 \cdot c^2$$

Ans: D

$$09. \quad \left[\left(\frac{1}{4} \right)^2 - \left(\frac{1}{4} \right)^3 \right] \times 2^6$$

$$= \left[\frac{1}{16} - \frac{1}{64} \right] \times 64$$

$$= \left[\frac{4-1}{64} \right] \times 64 = 3$$

Ans: C

$$10. \quad \left(\frac{a^9}{x^b} \right)^{a^2+ab+b^2} \cdot \left(\frac{x^b}{xc} \right)^{b^2+bc+c^2} \cdot \left(\frac{xc}{xa} \right)^{c^2+ca+a^2}$$

$$= (a-b)(a^2+ab+b^2) \cdot (b-c)(b^2+bc+c^2) \cdot (c-a)(c^2+ca+a^2)$$

$$= a^3 - b^3 + b^3 - c^3 + c^3 - a^3$$

$$= x$$

$$= x^0$$

$$= 1$$

Ans: A

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Ans: A

11. SMA-2
2

12. $a^2 = 16 \Rightarrow a = 4.$

Ans: A

$\therefore a^{-1} = \frac{1}{a} = \frac{1}{4}$

13. $x^{-2} = \frac{1}{5^2} \Rightarrow x = 5$

Ans: A

14. ~~$x^3 \cdot y^3 = z^5$~~

$\Rightarrow x^3 \cdot y^3 = z^5$

$\Rightarrow (xy)^3 = z^5$

Ans: D

$\Rightarrow xy = z^{\frac{5}{3}}$

15. $a^{8-2} = a^p \Rightarrow p = 6$

Ans: B

16. $m^{n-2m} = m^{-3}$

$\Rightarrow n = 3$

Ans:

17. $\left(\frac{m^3}{n^2}\right)^{-2} \times \left(\frac{n^5}{m}\right)^{-1}$

$= \left(\frac{m^{-6}}{n^{-4}}\right) \times \frac{n^{-5}}{m^{-1}}$

$= m^{-6+1} \times n^{-5+4}$

$= m^{-5} \times n^{-1}$

Ans:

$= \phi$

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5

$$\begin{aligned}
 19. & (a^3 \cdot b^2)^2 \div a^{-4} \cdot b^3 \\
 &= a^6 \cdot b^4 \div a^{-4} \cdot b^3 \\
 &= a^{6+4} \cdot b^{-4-3} \\
 &= a^{10} \cdot b^{-7} \\
 &= \frac{a^{10}}{b^7}
 \end{aligned}$$

Ans: —

$$20. a^3 \cdot b^3 \cdot a^2 \cdot b^{-4} = a^m \cdot b^n$$

$$\Rightarrow a^{11} \cdot b^{-1} = a^m \cdot b^n$$

$$\Rightarrow m+n = 11-1 = 10$$

Ans: —

ADVANCED LEVEL

Q1.

01. Conceptual

Ans: A, B, C, D

02.

$$\begin{aligned}
 \frac{2n \cdot 5 \cdot 3^9}{3 \cdot 3 \cdot 3} &= 3^3 \\
 3 \cdot \frac{16}{3} & \\
 2n+5+9-1-16 &= 3 \\
 \therefore 3 &
 \end{aligned}$$

$$\Rightarrow 2n-3 = 3$$

$$\Rightarrow n = 3 \text{ or } \sqrt[4]{81}$$

Ans: B, D

03.

$$\sqrt[3]{|1+3+9+27+81|} = \sqrt{1+1} = 11 \text{ or } \sqrt{11^2}$$

Ans: B, C

04.

$$a^{3/2} = \sqrt{a^3} = a\sqrt{a} = a \cdot a^{1/2}$$

Ans: A, C, D

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$$\begin{aligned} 05 \quad & 3^{-5} \cdot m \cdot n^2 = P \\ & \Rightarrow 3^{-5} \cdot n^2 = P \\ & \Rightarrow m \cdot n^2 = P \end{aligned}$$

Ans: C

06. Assertion: Conceptual (True)
Reason: Conceptual (True)

Ans: A

07. Assertion: Conceptual (False)
Reason: Conceptual (False)

Ans: A

08. Assertion: Conceptual (False)
Reason: Conceptual (True)

Ans: A

09. Assertion: Conceptual (True)
Reason: Conceptual (True)

Ans: A

10. Assertion: Conceptual (True)
Reason: Conceptual (True)

Ans: A

11. Assertion: Conceptual (True)
Reason: Conceptual (True)

12. Assertion: Conceptual (True)
Reason: Conceptual (True)

Ans: A

13. Assertion: Conceptual (True)
Reason: Conceptual (True)

Ans: A

14. Assertion: Conceptual (True)
Reason: Conceptual (True)

Ans: A

15. Assertion: Conceptual (True)
Reason: Conceptual (True)

Ans: A



16. Statement I:

$$x^{2017} \times \frac{1}{x^{2016}}$$

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$$= x^{2017-2016}$$

$$= x$$

$$= x^1 \text{ (True)}$$

Statement II: Conceptual (True)

$$\text{Statement I: } a^m = a^n \Rightarrow m = n \text{ (True)}$$

17 Statement I:

$$x^{x+2} = 4x-3$$

$$\Rightarrow \left(\frac{3}{2}\right)^{x+2} = 2$$

$$\Rightarrow \frac{3^{x+6}}{2} = 2$$

$$\Rightarrow 3^{x+6} = 4x-3$$

$$\Rightarrow 3^{x+6} = 4x-3$$

$$\Rightarrow 4x-3 \in 6+3$$

$$\Rightarrow x = 9 \text{ (True)}$$

Ans: A

18

$$\frac{3^{n+2} \cdot 3^{2n-1}}{4n-3} = \frac{3^{n+2+2n-1}}{4n-3} = \frac{3^{3n+1}}{4n-3}$$

$$= \frac{(3n+1) - (4n-3)}{3} = \frac{3n+1-4n+3}{3} = \frac{4-n}{3}$$

19.

$$= \frac{2^{a+3} \cdot 3^{3a-1}}{6^{a-2}}$$

$$= \frac{2^{a+3} \cdot 3^{3a-1}}{(2 \cdot 3)^{a-2}}$$

$$= \frac{2^{a+3} \cdot 3^{3a-1}}{2^{a-2} \cdot 3^3}$$

$$= \frac{(a+3) - (a-2)}{2} \cdot \frac{(3a-1) - (a-2)}{3} = \frac{2}{2} \cdot \frac{2a+1}{3} = \frac{2a+1}{3}$$

Ans: —

20.

$$\begin{aligned} \frac{3^{2x-1}}{2} \cdot 4^{x+2} &= 8^{2x} \\ \Rightarrow \frac{3^{2x-1}}{2} \cdot \binom{2}{2}^{x+2} &= \binom{3}{2}^{2x} \\ \Rightarrow \frac{3^{2x-1}}{2} \cdot 2^{2x+4} &= 2^{6x} \\ \Rightarrow 5x+3 &= 6x \\ \Rightarrow 5x+3 &= 6x \\ \Rightarrow x &= 3 \end{aligned}$$

Ans: —

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21

$$x^a - b^2 + b^2 - c^2 + c^2 - a^2 = a^0 = 1$$

Ans: C

22

$$\begin{aligned} \left(\frac{5}{2}\right)^{-5} \cdot \left(\frac{2}{3}\right)^{-5} \\ = \left(\frac{5}{2} \times \frac{2}{3}\right)^{-5} \\ = \left(\frac{5}{3}\right)^{-5} = \left(\frac{3}{5}\right)^5 = \end{aligned}$$

Ans: —

23

$$\begin{aligned} \frac{2^{2x-1}}{5} &= 25^{x+2} \\ \Rightarrow \frac{2^{2x-1}}{5} &= 5^{2x+4} \\ \Rightarrow 2^{2x-1} &= 2^{2x+4} \end{aligned}$$

Ans: —

24

$$\begin{aligned} 4^{x-2} &= 8^{2x+1} \\ = 2^{2x-4} &= 2^{6x+3} \\ \Rightarrow 2^{2x-4} &= 6x+3 \\ \Rightarrow 4x &= -4-3 \\ \Rightarrow x &= -\frac{7}{4} \end{aligned}$$

Ans: —

25.

$$\frac{3x}{2} = 16 \cdot 2^x$$

$$\Rightarrow \frac{3x}{2} = 4 + x$$

$$\Rightarrow 3x = 4 + 2x$$

$$\Rightarrow 2x = 4$$

$$\Rightarrow x = 2$$

Ans: 2

26

$$3^{x+2} = 18$$

$$\Rightarrow 3^x \cdot 3^2 = 18$$

$$\Rightarrow 3^x \cdot 9 = 18$$

$$\Rightarrow 3^x = 2$$

Ans: 2

27

$$8^{x-1} = 2^{x+3}$$

$$\Rightarrow \frac{3^{x-3}}{2} = 2^{x+3}$$

$$\Rightarrow 3^{x-3} = 2^{x+3}$$

$$\Rightarrow 2x = 6$$

$$\Rightarrow x = 3$$

Ans: 3

28

$$29. a) 5^{-5} = \frac{1}{5^5}$$

$$b) 6^{-6} \times 6^6 = 6^{-6+6} = 6^0 = 1$$

$$c) \text{ If } x^3 = 7^3 \Rightarrow x = 7$$

$$d) 2^1 = 2^1 = 2$$

Ans: 5, 2, 3, 2

9

29

$$a) \frac{2^{10}}{2^{-10}} = 2^{10+10} = 2^{20}$$

$$b) 6^{18} = (2 \times 3)^{18} = 2^{18} \times 3^{18}$$

$$c) 2^x = 16 \Rightarrow x = 4$$

$$d) 5^0 - 6^0 = 1 - 1 = 0$$

Ans: s, y, t, a

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LEARNER'S TASKCUR'S

$$01. \left(-\frac{2}{5}\right)^{-3} = \left(\frac{-5}{2}\right)^3 = -\frac{125}{8}$$

Ans: B

$$02. (-n^2)^2 \times (-n^2)^3$$

$$= n^4 \times -n^6 = -n^{10}$$

Ans: A

$$03. x = a^m, y = a^n, \therefore x^m = a^{nm}$$

Ans: A

$$04. (x^{m-n})^p \cdot (x^{n-p})^m \cdot (x^{p-m})^n$$

$$= x^{mp-np+nm-pm+pn-mm} = x^0 = 1$$

Ans: B

$$05. x^0 = 1$$

Ans: C

$$06. 20 \cdot (x-y)^4$$

Ans: A

$$07. (2010)^{2010}$$

Ans: B

$$08. \left(-\frac{1}{3}\right) \times 6^0 = (-1) \times 6^0 = 0$$

Ans: D

$$09. (-1)^{2014} = 1 \text{ since } 2014 \text{ is Even.}$$

Ans: A

$$10. \quad a^3 - b^5 = 5^3 - 3^5$$

$$= 125 - 243$$

$$= -118$$

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Ans: D

$$11. \quad \frac{a^{10}}{a^{12}} = a^{10-12} = a^{-2}$$

Ans: C

$$12. \quad \frac{3^2}{4} - 4^8$$

$$= 4^9 - 4^8 = 4^8(4-1) = 3 \times 4^8$$

$$= 3 \times 2^{16}$$

Ans: B

$$13. \quad 8^{2x} \times 2^2 = 2^6$$

$$\Rightarrow 2^{3x+2} = 2^6 \Rightarrow x = \frac{4}{3}$$

Ans: B

$$14. \quad 96326000000$$

$$= 96326 \times 10^6$$

$$= 9.6326 \times 10^{10}$$

Ans: B

JEE MAINS LEVEL

$$01. \quad \frac{1}{2} \times (3^x - 3^{x-1}) = 81$$

$$3^x - \frac{3^x}{3} = 162 \Rightarrow x = 5 \text{ (option verification)}$$

Ans: D

$$02. \quad 0.000019$$

$$= \frac{19}{1000000} = 19 \times 10^{-6}$$

$$= 1.9 \times 10^{-5}$$

Ans: A

$$03. \quad (x^{-1} + y^{-1})^{-1} = \left(\frac{1}{x} + \frac{1}{y} \right)^{-1} = \left(\frac{x+y}{xy} \right)^{-1} = \frac{xy}{x+y}$$

Ans: C

$$\left[\sqrt{x}^{2-3n+4+3n-3} \right]^3$$

12

$$= \left(\frac{3}{x} \right)^3 = x^9$$

Ans: D

$$3^{x-1} = 3^2$$

$$4^{y+2} = 4^3$$

$$\therefore \frac{x}{y} = 3$$

$$\Rightarrow x = 3$$

$$\Rightarrow y = 1$$

Ans: B

$$\left\{ \left(\frac{3}{2} \right)^{-1} \div \left(-\frac{2}{5} \right)^{-1} \right\}$$

$$= \left\{ \frac{2}{3} \div \left(-\frac{5}{2} \right) \right\} = \frac{2}{3} \times -\frac{2}{5} = -\frac{4}{15}$$

Ans: D

$$\frac{5x-3}{19x+2} = \frac{3}{5}$$

$$\Rightarrow 25x - 15 = 57x + 6$$

$$\Rightarrow 32x = -21$$

$$\Rightarrow x = -\frac{21}{32}$$

Ans: A

19.

$$x+y = 5$$

$$\Rightarrow x^2 + y^2 + 2xy = 25$$

$$\Rightarrow 10 + 2xy = 25$$

$$\Rightarrow xy = \frac{15}{2} = 7\frac{1}{2}$$

Ans: A

$$10. (50.5)^2 - (49.5)^2$$

$$= (50.5 + 49.5)(50.5 - 49.5)$$

$$= 100 \times 1$$

$$= 100$$

Ans: B

04.
$$\left[x^{2-3n+4+3n-3} \right]^3$$

$$= \left(x^3 \right)^3 = x^9$$

Ans: D

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05.
$$3^{x-1} = 3^2$$

$$y+2 = 4^3$$

$$\therefore \frac{x}{y} = 3$$

$$\Rightarrow x = 3$$

$$\Rightarrow y = 1$$

Ans: B

06.

$$\left\{ \left(\frac{3}{2} \right)^{-1} \div \left(-\frac{2}{5} \right)^{-1} \right\}$$

$$= \left\{ \frac{2}{3} \div \left(-\frac{5}{2} \right) \right\} = \frac{2}{3} \times \frac{-2}{5} = -\frac{4}{15}$$

Ans: D

08

$$\frac{5x-3}{19x+2} = \frac{3}{5}$$

$$\Rightarrow 25x-15 = 57x+6$$

$$\Rightarrow 32x = -21$$

$$\Rightarrow x = -\frac{21}{32}$$

Ans: A

09.

$$x+y = 5$$

$$\Rightarrow x^2+y^2 + 2xy = 25$$

$$\Rightarrow 10 + 2xy = 25$$

$$\Rightarrow xy = \frac{15}{2} = 7\frac{1}{2}$$

Ans: A

10.

$$(50.5)^2 - (49.5)^2$$

$$= (50.5 + 49.5)(50.5 - 49.5)$$

$$= 100 \times 1$$

$$= 100$$

Ans: B

12. $2^{0.64} + 0.36 = \frac{1}{2} = 2$

Ans: B

13. $a^3 \times b^2 = a^5 \times b$

$\Rightarrow b = a^2$

Ans: A

The value of b is a^2

14. $\frac{1}{2^2} + \frac{1}{3^3} = \frac{1}{4} + \frac{1}{27}$

$= \frac{31}{108}$

Ans: B

15. ~~$x^4(x-x^4)$~~ $= x - x^4$

otherwise, $\frac{x^4 \times x^7}{x^3} = x^8$

Ans: B

16. $3^4 \times x = 729 = 3^6$

$\therefore x = 3^2 = 9$

Ans: —

17. $x^0 = 1$

Ans: D

18. $3^{2x-1} = 3^3$

$\Rightarrow x = 2$

Ans: C

19. $8x^6 \cdot 9x^2 = 72x^8$

Ans: —

20. $a^{3+4} \cdot b^{-2-4} = \frac{a^7}{b^6}$

Ans: —

21. $\frac{x^2}{p^2 \cdot q^{-3}} \times \frac{x^6}{p^2 \cdot q^2} = \frac{x^8}{p^4 \cdot q^{-1}} = p^{-4} \cdot q \cdot x^8$

Ans:

14

$$22. (ab)^2 = \frac{c}{d^3}$$

$$\Rightarrow ab = \frac{c^{1/2}}{d^{3/2}}$$

$$(ab)^3 = (ab)^2 \cdot (ab)$$

$$= \frac{c}{d^3} \times \frac{c^{1/2}}{d^{3/2}}$$

$$= \frac{c^{3/2}}{d^{9/2}}$$

ADVANCED LEVEL QUESTIONS

01. $n-2n+4n = m^p$

$\Rightarrow 3n = m^p$

$\Rightarrow 3n = p$

Ans: C

02. $\frac{x^{-6}}{y^{-4}} \times \frac{y^{15}}{x^{-3}} = \frac{y^{19}}{x^6} = x^{-6} \cdot y^{19}$

Ans: C

03. $8^{2/3} = (2^3)^{2/3} = 2^2 = 4$ (or) $\sqrt[3]{64} = (2^6)^{1/3} = 2^2 = 4$

Ans: A, B, C

04. $2^9 + 14 = 2^3$ or 2^{14+9} or $2^9 \times 2^4$

Ans: A, C, D

05. $\frac{2n \cdot 2 \cdot 3 \cdot 3 \cdot 3 \cdot 3 \cdot 3}{3 \cdot 3 \cdot 3 \cdot 3 \cdot 3} = \frac{2^2 \cdot 3^5}{3^5} = 2^2 = 4$



$\Rightarrow n-m = -1$

$\Rightarrow m-n = 1$

$\Rightarrow \frac{3^n (9-1)}{3^m \cdot 2} = \frac{1}{27}$

$\Rightarrow \frac{3^{n-3m}}{3} = \frac{1}{27}$

$\Rightarrow 3^{n-3m-1} = 3^{-3}$

Ans: A

06 Assertion: True

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Reason: Conceptual (True)

Ans: A

07. Assertion: $\frac{7^3}{7^4} = \frac{1}{7} = 7^{-1}$ (True)

Ans: A

Reason: Conceptual (True)

08 Assertion: False

Reason: ~~False~~ True

Ans: B

09. Statement I: $\binom{3}{2}^2 = 2^6 = 64$ (True)
Statement II: $2^2 \cdot 3^3 = 3^{2+3} = 3^5$ (True)

Ans: A

Statement II: Conceptual (True)

10. Statement I: Conceptual (True)

Statement II: $2^{2+2} = 4^{2-3}$

$$\Rightarrow 2^{2+6} = 4^{2-3}$$

$$\Rightarrow 2^{2+6} = 4^{2-3}$$

$$\Rightarrow 2^8 = 9$$

$$\Rightarrow 2^8 = 9/2 \text{ (False)}$$

Ans: C

11. Statement I: ${}^R \sqrt{y} = y^R$

$$\Rightarrow {}^R \sqrt{y} = y$$

$$\text{Now, } \left(\frac{y}{R}\right)^{\frac{R}{y}} = \left(\frac{y}{y/R}\right)^{\frac{R}{y}} = \left(1 - \frac{y}{R}\right)^{\frac{R}{y}} = {}^R \sqrt{1 - \frac{y}{R}} \text{ (True)}$$

Statement I:

$$2^x = 4^y = 8^z$$

$$\Rightarrow 2^x = 2^{2y} = 2^{3z}$$

$$\Rightarrow x = 2y = 3z$$

Given $xyz = 288$

$$\Rightarrow x \left(\frac{x}{2}\right) \left(\frac{x}{3}\right) = 288$$

$$\Rightarrow x^3 = 2^6 \times 3^3$$

$$\Rightarrow x = \sqrt[3]{2^6 \times 3^3} = (2 \times 3)^2$$

$$\therefore x = 12, y = 6, z = 4$$

$$\therefore \frac{1}{2x} + \frac{1}{4y} + \frac{1}{8z} = \frac{1}{24} + \frac{1}{24} + \frac{1}{32}$$

$$= \frac{11}{96} \quad (\text{True}) \quad \text{Ans: A}$$

12. $x^0 = 1$

13. $\frac{-5+2x+1}{2} = 2$

$$\Rightarrow 2x - 4 = 6$$

$$\Rightarrow x = 5$$

14. 0.000939478

$$= \frac{939478}{10^9} = 939478 \times 10^{-9}$$

$$= 9.39478 \times 10^5 \times 10^{-9}$$

$$= 9.39478 \times 10^{-4}$$

Ans: A

15.

$$3^{x+5} = 81^{x-1}$$

$$\Rightarrow 3^{x+5} = 3^{4x-4}$$

$$\Rightarrow x+5 = 4x-4$$

$$\Rightarrow 3x = 9$$

$$\Rightarrow x = 3$$

Ans: 3

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16.

$$100 - 100 = 2^0 = 1$$

Ans: 1

17.

$$\frac{3x-3}{2} = x+3$$

$$\Rightarrow 3x-3 = 2x+6$$

$$\Rightarrow 2x = 9$$

$$\Rightarrow x = 3$$

Ans: 3

18.

a) $2^{100} = 100^2$

b) $(12^0 - 11^0) (3^1 - 1^3) = (1-1)(3-1) = 0$

c) $(128)^{\frac{5}{7}} = (2^7)^{\frac{5}{7}} = 2^5 = 32$

d) $5^x = 25^y = 625$

$$\Rightarrow 5^x = 5^{2y} = 5^4$$

$$\Rightarrow x = 4, y = 2$$

Now, $x^2 - y^2 = 4^2 - 2^2 = 16 - 4 = 12$

Ans: E, P, x, y

17. a) $A^{(2-1+1)} = 2^0$

b) $A^{(2+2)} = 2^4 = 16$

c) $2^4 = 16$ or $2^2 = 4$

d) $2^2 = 4$ or $1 = 1$

Ans: a, b, c, d

THE END

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18

19. a) $2^{10 - (-10)} = 2^{20}$

b) $6^{18} = (2 \times 3)^{18} = 2^{18} \times 3^{18}$

c) $2^x = 16 \Rightarrow x = 4$

d) $5^6 - 6^0 = 1 - 1 = 0$

Ans: s, u, t, q

\Rightarrow THE END \in